

Name.....  
Group#.....#.....

الفصل الخامس

College of Electronic Technology

Electromagnetic I-2020

Time: 120 minutes

final Exam

Total Marks is (60)

Answer these questions as the best of your knowledge:

Q1) (a) State Maxwell's equations for static EM fields?

(b) Find the maximum rate of change in scalar field:

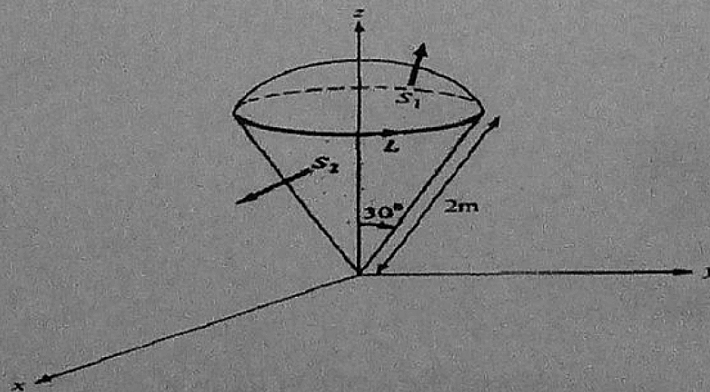
$$W = 10r \sin^2 \theta \cos \phi$$

Q2) Let  $A = \rho \cos \theta a_\rho + \rho z^2 \sin \phi a_\phi$

(a) Transform A into rectangular coordinates and calculate its magnitude at point (3, -4, 0).

b) If A is solenoidal at Z plane what is the value of  $\phi$  should be?

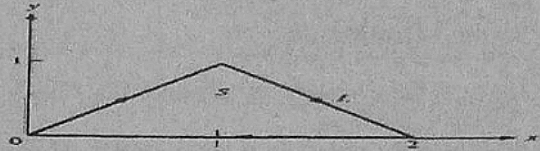
(c) For the ice-cream cone Fig-d express  $dl$ .  $ds_1$ .  $ds_2$ ?



Q3)

Given that  $\mathbf{F} = x^2y \mathbf{a}_x - y \mathbf{a}_y$ , find

- (a)  $\oint_L \mathbf{F} \cdot d\mathbf{l}$  where  $L$  is shown in Figure 3.29.  
 (b)  $\int_S (\nabla \times \mathbf{F}) \cdot d\mathbf{S}$  where  $S$  is the area bounded by  $L$ .  
 (c) Is Stokes's theorem satisfied?



Q4)

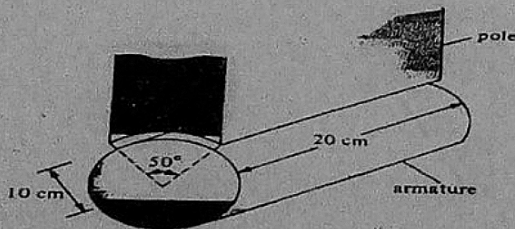
In a certain region, the electric field is given by

$$\mathbf{D} = 2\rho(z + 1)\cos\phi \mathbf{a}_\rho - \rho(z + 1)\sin\phi \mathbf{a}_\phi + \rho^2 \cos\phi \mathbf{a}_z \mu\text{C}/\text{m}^2$$

- (a) Find the charge density.  
 (b) Calculate the total charge enclosed by the volume  $0 < \rho < 2$ ,  $0 < \phi < \pi/2$ ,  $0 < z < 4$ .  
 (c) Confirm Gauss's law by finding the net flux through the surface of the volume in (b).

Q5) The electric motor shown in Figure 7.32 has field

$$\mathbf{H} = \frac{10^6}{\rho} \sin 2\phi \mathbf{a}_\rho \text{ A/m}$$



(a)

Calculate the flux per pole passing through the air gap if the axial length of the pole is 20 cm.

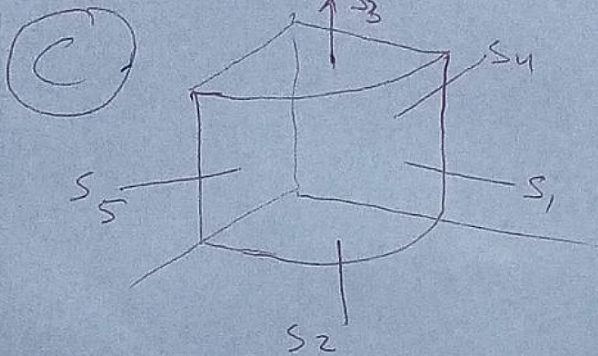
(b) Determine  $\mathbf{J}$  at  $(1, 45, 0)$

(c) Determine  $\mathbf{B}$

the end of question

24) (a)  $\rho_v = \nabla \cdot \bar{D} = 4(z+1) \cos \phi - (z+1) \cos \phi + 0$   
 $= 3(z+1) \cos \phi \frac{\mu C}{m^2}$

(b)  $Q_{enc} = \int \rho_v dv = \iiint 3(z+1) \cos \phi \rho d\phi d\rho dz$   
 $= 3 \int_0^2 \rho d\rho \int_0^4 (z+1) \int_0^{\pi/2} \cos \phi d\phi = 3(z) \left( \frac{z^2}{2} + z \right) \Big|_0^4$   
 $\left( \sin \phi \Big|_0^{\pi/2} \right) = 72 \mu C$  12 marks



$\psi = \psi_1 + \psi_2 + \psi_3 + \psi_4 + \psi_5$   
 $= \oint \bar{D} \cdot d\bar{S}$   
 الجهد الكلي الناتج عن الشحنة

For  $S_1 \rightarrow \rho = 2, dS = \rho d\phi dz \bar{a}_\rho$   
 $\therefore \psi_1 = \iint 2\rho(z+1) \cos \phi \Big|_{\rho=2} = 2(z) \int_0^4 (z+1) dz \int_0^{\pi/2} \cos \phi d\phi$   
 $= 4(12)(1) = 48$

For  $S_2 \Rightarrow z=0, dS = \rho d\phi d\rho (-\bar{a}_z)$   
 $\psi_2 = - \iint \rho^2 \cos \phi \cdot \rho d\phi \cdot d\rho = - \int_0^2 \rho^3 d\rho \int_0^{\pi/2} \cos \phi d\phi$   
 $= - \frac{\rho^4}{4} \Big|_0^2 (1) = -4$

For  $S_3 \Rightarrow z=4, dS = \rho d\phi d\rho \bar{a}_z \Rightarrow \psi_3 = 4$

For  $S_4 \Rightarrow \phi = \frac{\pi}{2}, dS = d\rho dz \bar{a}_\phi$   
 $\psi_4 = \iint \rho(z+1) \sin \phi d\rho dz \Big|_{\phi=\pi/2} = \left( \int_0^4 \rho d\rho \int_0^4 (z+1) dz \right) \sin \frac{\pi}{2}$   
 $= -24$

For  $S_5 \Rightarrow \phi = 0, dS = d\rho dz (-\bar{a}_\phi), \psi_5 = \iint \rho(z+1) \sin \phi d\rho dz \Big|_{\phi=0} = 0$   
 $\psi_{total} = 24 \mu C$

2.5

Electromagnetic I exam Solution  
Spring 2019

(1)

Q1

(a)

$$\nabla \cdot \vec{D} = \rho_v, \nabla \cdot \vec{B} = 0, \nabla \times \vec{E} = 0, \nabla \times \vec{H} = \vec{J}$$

(b)

The gradient

$$\nabla W = 10 \sin^2 \theta \cos \phi \vec{a}_r + 10 \sin 2\theta \cos \phi \vec{a}_\theta - 10 \sin \theta \sin \phi \vec{a}_\phi$$

(3)

12 marks

~~(c)~~

Solenoidal  $\rightarrow \nabla \cdot \vec{A} = 0$ , potential  $\rightarrow \nabla \times \vec{A} = \vec{J}$

Q3

$$(a) \oint_C \vec{F} \cdot d\vec{l} = \left( \int_1 + \int_2 + \int_3 \right) \vec{F} \cdot d\vec{l}$$

at (1)  $y = x, dy = dx, dl = dx \vec{a}_x + dy \vec{a}_y$

$$\therefore \int_1 \vec{F} \cdot d\vec{l} = \int_0^1 x^3 dx - x dx = \boxed{-\frac{1}{4}}$$

at (2)  $y = -x + 2, dy = -dx, dl = dx \vec{a}_x + dy \vec{a}_y$

$$\therefore \int_2 \vec{F} \cdot d\vec{l} = \int_0^2 (-x^3 + 2x^2 - x + 2) dx = \boxed{\frac{17}{12}}$$

at (3)  $\int_3 \vec{F} \cdot d\vec{l} = \int_0^1 x^2 y dx \Big|_{y=0} = 0 \Rightarrow \boxed{\frac{7}{6}}$

$$(b) \nabla \times \vec{F} = -x^2 \vec{a}_z, d\vec{s} = dx dy (-\vec{a}_z)$$

$$\int (\nabla \times \vec{F}) \cdot d\vec{s} = - \iint (-x^2) dx dy = \int_0^1 \int_0^x x^2 dy dx$$

$$+ \int_0^2 \int_1^2 x^2 dy dx = \frac{x}{4} \Big|_0^1 + \int_1^2 x^2 (-x+1) dx = \frac{7}{6}$$

(c)

Yes

Swatshin

2 marks

Q1

$$(a) \psi = \int \vec{B} \cdot d\vec{s} = \mu_0 \int_{z=0}^{0.2} \int_{\phi=0}^{50} \frac{10^6}{\rho} \sin 2\phi \rho d\phi dz$$

$$\psi = 4\pi \times 10^{-7} \times 10^6 (0.2) \left( -\frac{\cos 2\phi}{2} \right) \Big|_0^{50}$$

$$\psi = 1.1475 \text{ wb}$$

17 marks

$$(b) \vec{J} = \nabla \times \vec{H}$$

$$= \begin{bmatrix} 0 & 0 & 0 \end{bmatrix} \vec{a}_\rho + \begin{bmatrix} 0 & 0 & 0 \end{bmatrix} \vec{a}_\phi$$

$$+ \frac{1}{\rho} \begin{bmatrix} 0 & -\frac{1 \cdot 10^6}{2} \cos 2\phi & 0 \end{bmatrix} = \frac{2 \times 10^6}{\rho^2} \cos 2\phi \vec{a}_z$$

Q2

$$\vec{B} = \mu_0 \vec{H} = \frac{4\pi \times 10^{-7} \times 10^6}{\rho} \sin 2\phi \vec{a}_\rho$$

$$\vec{B} = \frac{4\pi}{10\rho} \sin 2\phi \vec{a}_\rho$$

End

Q2

$$ds_1 = r \sin \theta d\phi \cdot r d\theta \cdot \hat{a}_r = r^2 \sin \theta \cdot d\phi d\theta \cdot \hat{a}_r$$

$$ds_2 = r \cdot \sin \theta d\phi \cdot \hat{a}_\phi = r \cdot \sin \theta \cdot d\phi \cdot \hat{a}_\phi = \frac{r}{z} d\phi \cdot \hat{a}_\phi$$

$$ds_3 = r \cdot \sin \theta \cdot d\phi \cdot dr \cdot \hat{a}_\theta = r \cdot \frac{1}{z} \cdot d\phi \cdot dr \cdot \hat{a}_\theta$$

12 marks